

# NEUTRAL NATURALNESS



NATHANIEL CRAIG  
UCSB+RUTGERS



*BASED PRIMARILY ON WORK IN PROGRESS  
WITH SIMON KNAPEN & PIETRO LONGHI*

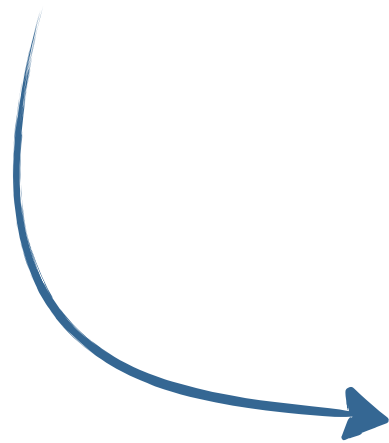
LANL SANTA FE SUMMER WORKSHOP 2014  
"LHC AFTER THE HIGGS" (DON'T PANIC)

# TODAY'S TALK

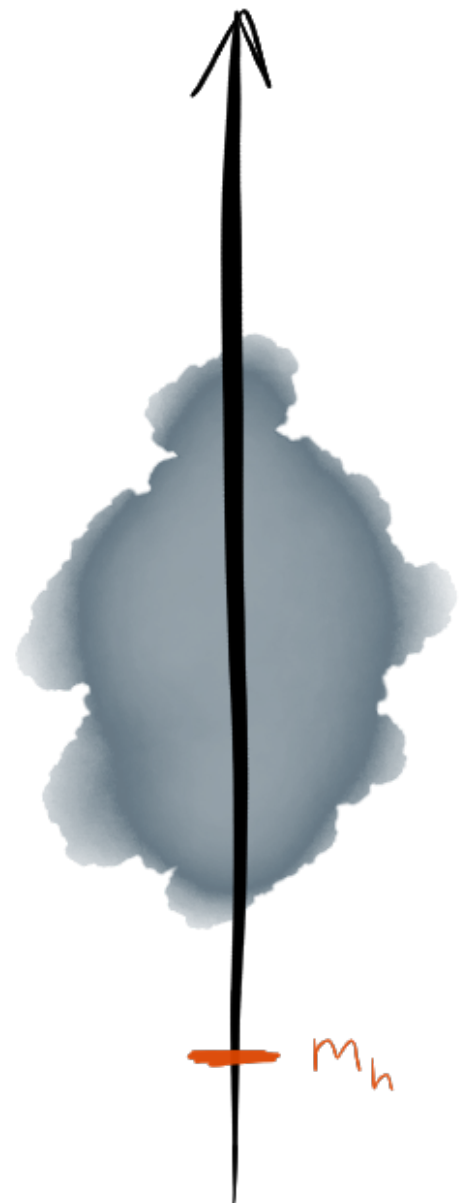
MISSING TOP  
PARTNER  
PROBLEM

"THE  
ORBIFOLD  
HIGGS"

BUT, WHAT  
ABOUT THE  
TWIN HIGGS?



# HIERARCHY PROBLEM!



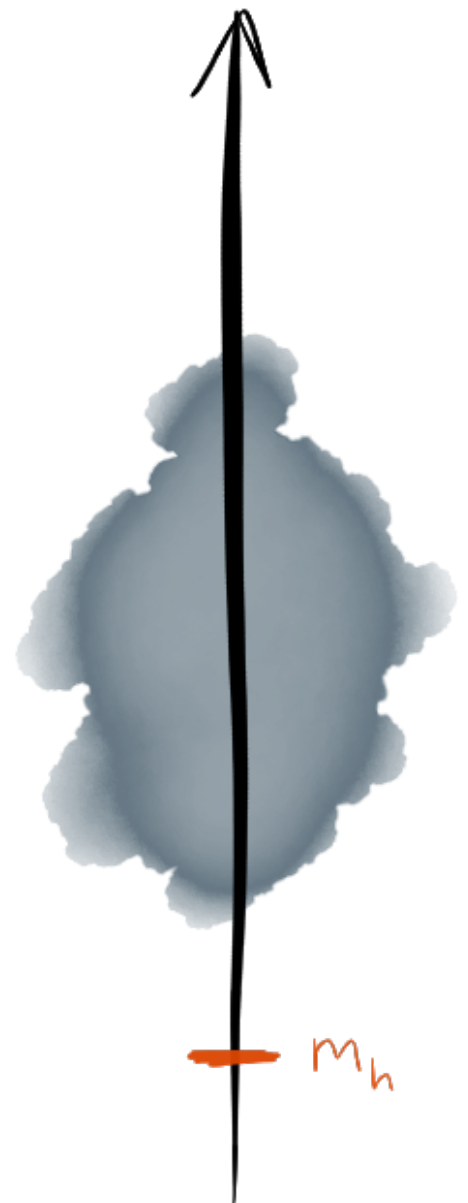
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QUADRATICALLY SENSITIVE TO  
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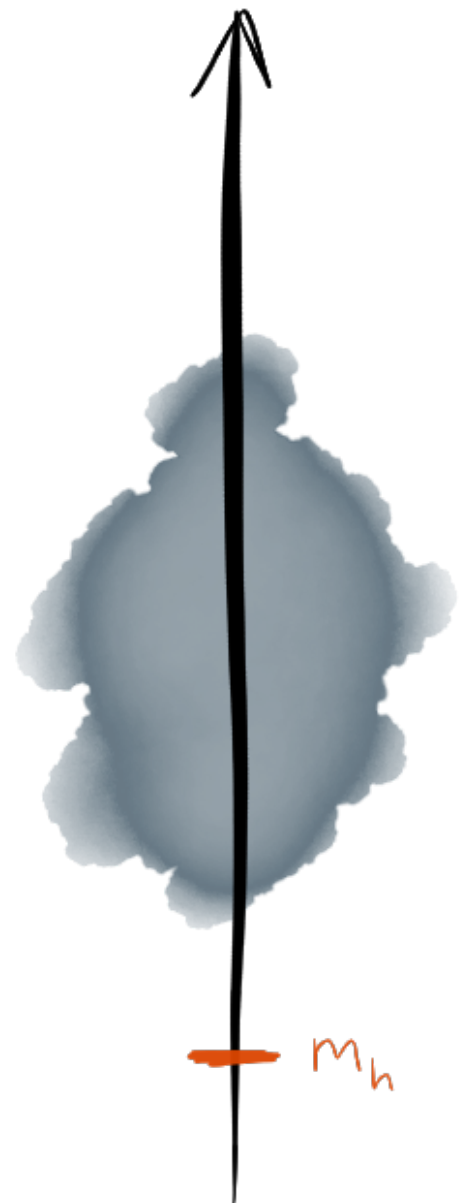
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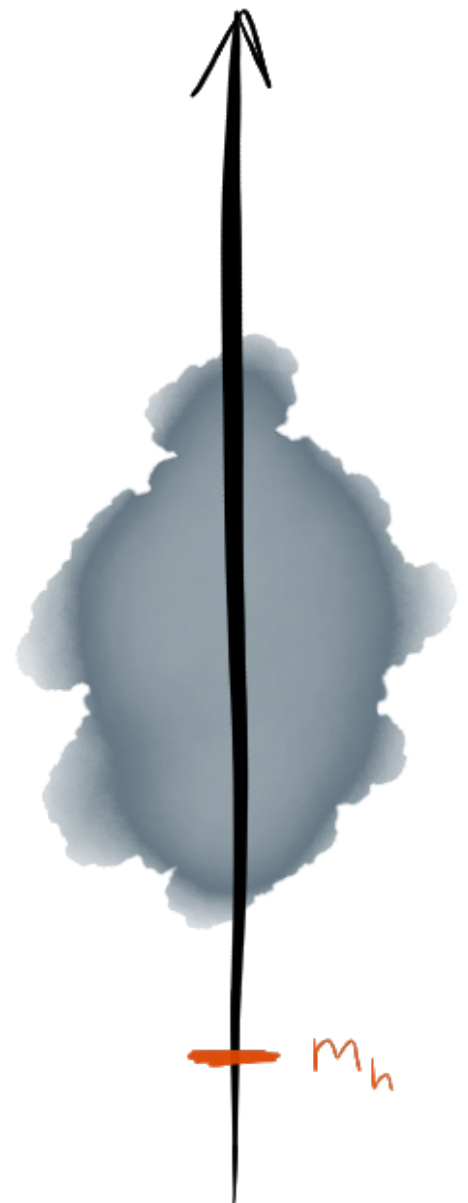
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**SYMMETRY** OR LOWERING THE  
**CUTOFF**.
- PURE CUTOFF SOLUTIONS PUSHED  
TO  $\sim 5$  TEV, DISFAVORED.



TOP PARTNER "THEOREM"



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- SYMMETRY PROTECTING HIGGS ACTS ON HIGGS ITSELF.

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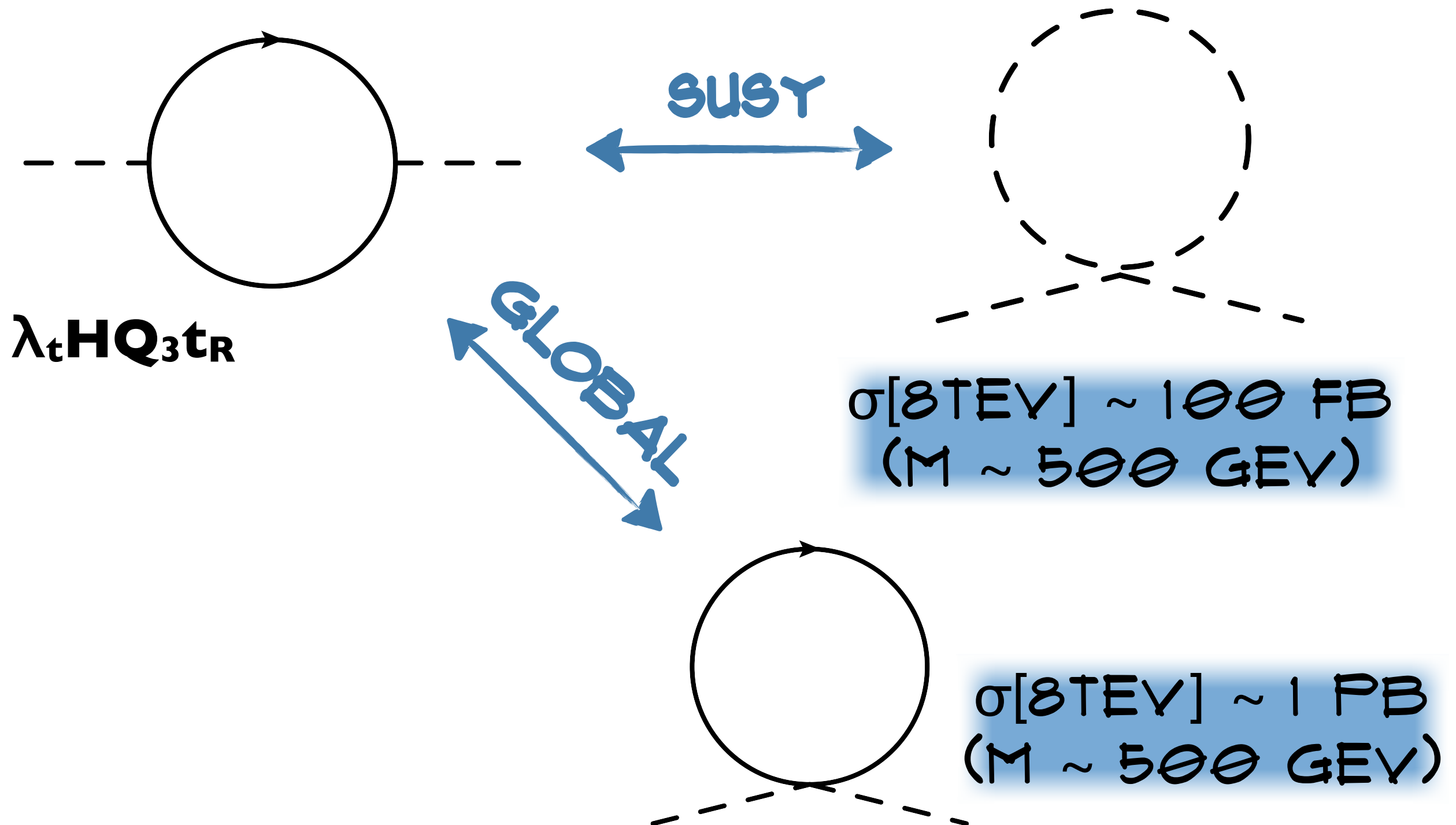
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- DECAY MODES VARY BUT GUARANTEED LARGE QCD CROSS SECTION.

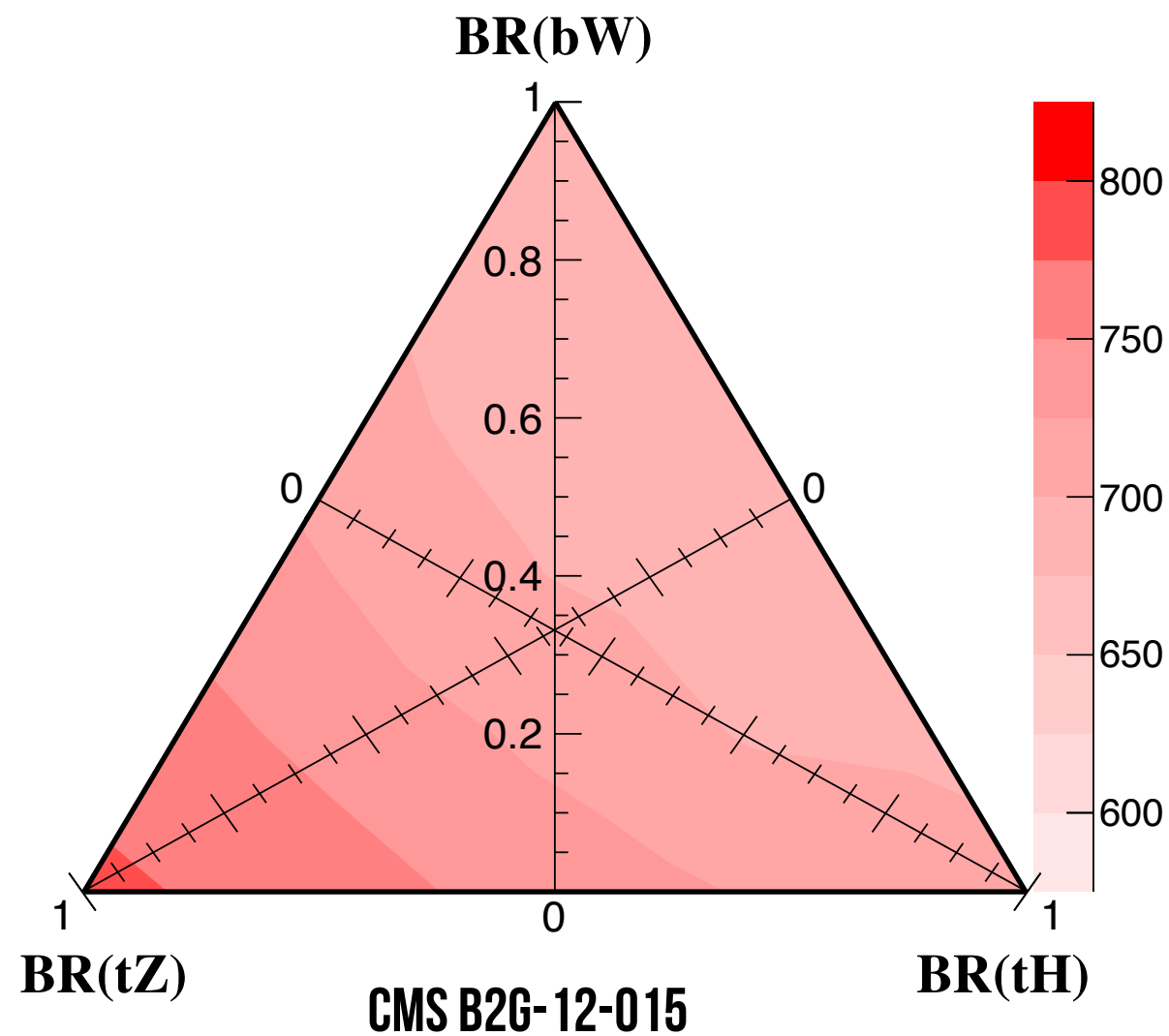
# THE TOP PARTNER THEOREM



# THE TOP PARTNER PROBLEM

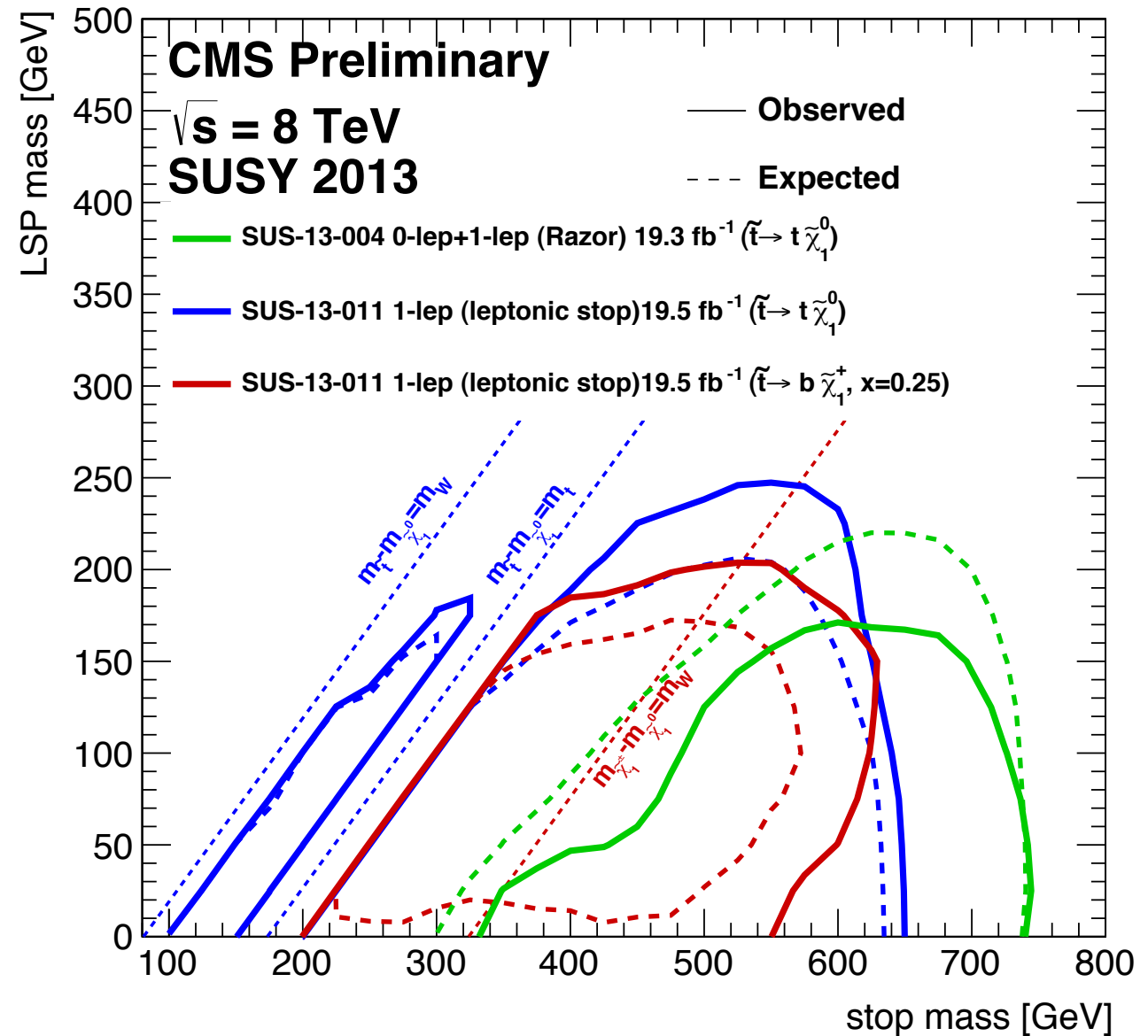
## GLOBAL SYMMETRY

CMS preliminary  $\sqrt{s} = 8 \text{ TeV}$   $19.6 \text{ fb}^{-1}$



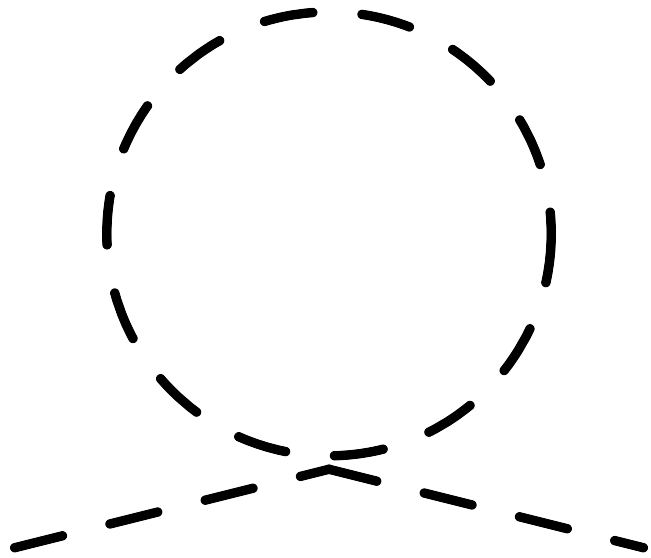
## SUPERSYMMETRY

$\tilde{t}\text{-}\tilde{t}$  production

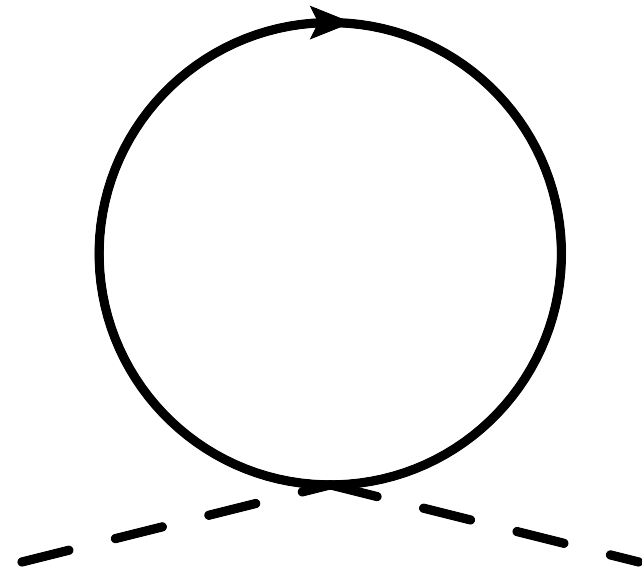




# NATURALNESS?



$$\delta m_H^2 = -\frac{3}{8\pi^2} \lambda_t^2 \tilde{m}_t^2 \log(\Lambda^2 / \tilde{m}_t^2)$$



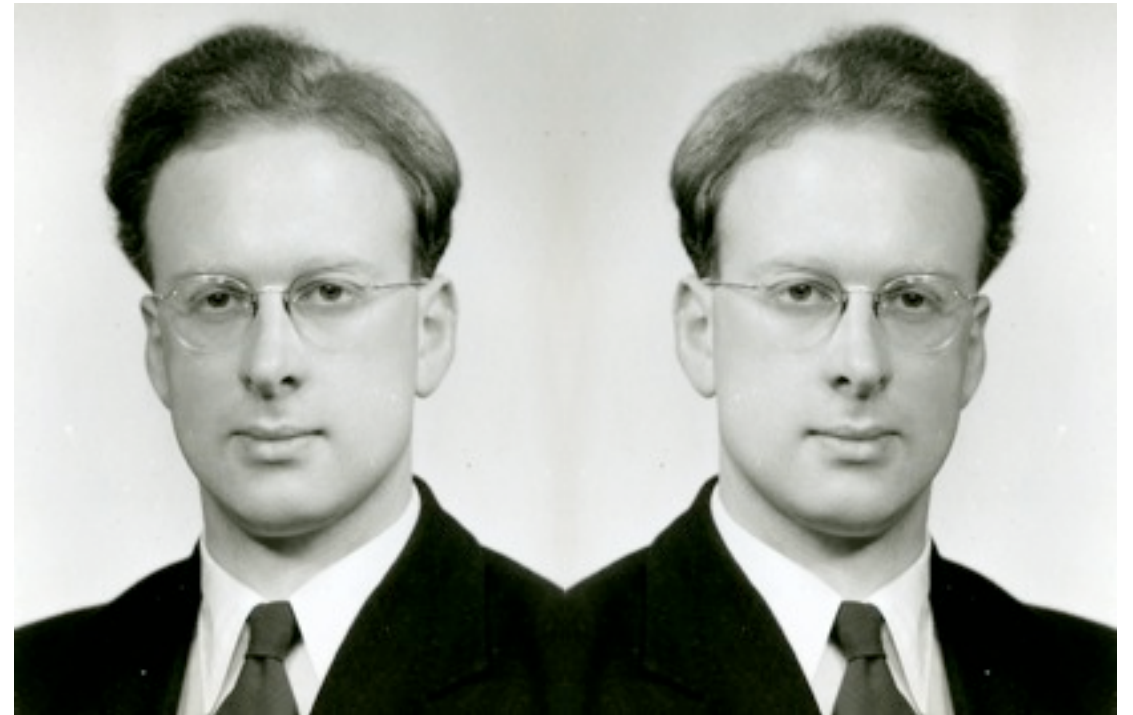
$$\delta m_H^2 = -\frac{3}{8\pi^2} \lambda_t^2 m_T^2 \log(\Lambda^2 / m_T^2)$$

Irreducible tuning:  $\sim 5\%$ . Complete model:  $\lesssim 0.1-1\%$

# BUT WHAT ABOUT...

## THE TWIN HIGGS

[Z. CHACKO, H.-S.  
GOH, R. HARNIK '05]



electroweak constraints are satisfied by construction. These models demonstrate that, contrary to the conventional wisdom, stabilizing the weak scale does not require new light particles charged under the Standard Model gauge groups.

SYMMETRY IS  $SM_A \times SM_B \times Z_2$

*\*SEE ALSO CHACKO'S TALK ON THURSDAY*

# THE TWIN HIGGS

CONSIDER A SCALAR  $H$  TRANSFORMING AS A FUNDAMENTAL UNDER A GLOBAL  $SU(4)$ :

$$V(H) = -m^2 |H|^2 + \lambda |H|^4$$

POTENTIAL LEADS TO SPONTANEOUS SYMMETRY BREAKING,

$$|\langle H \rangle|^2 = \frac{m^2}{2\lambda} \equiv f^2$$

$$SU(4) \rightarrow SU(3)$$

YIELDS SEVEN  
GOLDSTONE BOSONS.

UV:  $\lambda \gg 1$  NLSM;  $\lambda \lesssim 1$  LSM

# THE TWIN HIGGS

NOW GAUGE  $SU(2)_A \times SU(2)_B \subset SU(4)$ , w/  $H = \begin{pmatrix} H_A \\ H_B \end{pmatrix}$

US

TWINS

*Then 6 goldstones are eaten, leaving one behind.*

**EXPLICITLY BREAKS THE  $SU(4)$ ; EXPECT RADIATIVE CORRECTIONS.**

$$V(H) \supset \frac{9}{64\pi^2} (g_A^2 \Lambda^2 |H_A|^2 + g_B^2 \Lambda^2 |H_B|^2)$$

**BUT THESE BECOME  $SU(4)$  SYMMETRIC IF  $G_A = G_B$  FROM A  $Z_2$**

*Quadratic potential has accidental  $SU(4)$  symmetry.*

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# TWIN HIGGS SLOGAN

“HIGGS IS PSEUDO-GOLDSTONE OF  
THE ACCIDENTAL GLOBAL  
SYMMETRY OF QUADRATIC ACTION  
OBEYING DISCRETE SYMMETRY”\*

\*PLUS SYMMETRIC QUARTIC.

# THE TWIN HIGGS

ACHIEVE THIS PROTECTION FOR THE ENTIRE  
SM BY  $SM_A \times SM_B \times Z_2$

$SM_A = US$ ,  $SM_B = \text{TWIN SECTOR}$

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CRUCIALLY:  $\mathcal{L} \supset -y_t H_A Q_3^A \bar{u}_3^A - y_t H_B Q_3^B \bar{u}_3^B$



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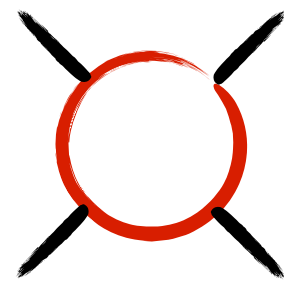
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*Explicit breaking generates one-loop  
quartic:*

$$V \supset \kappa (|H_A|^4 + |H_B|^4) \quad \kappa \sim \frac{y_t^4}{16\pi^2} \log(\Lambda/f)$$

*(only quadratic potential enjoys  $SU(4)$ )*

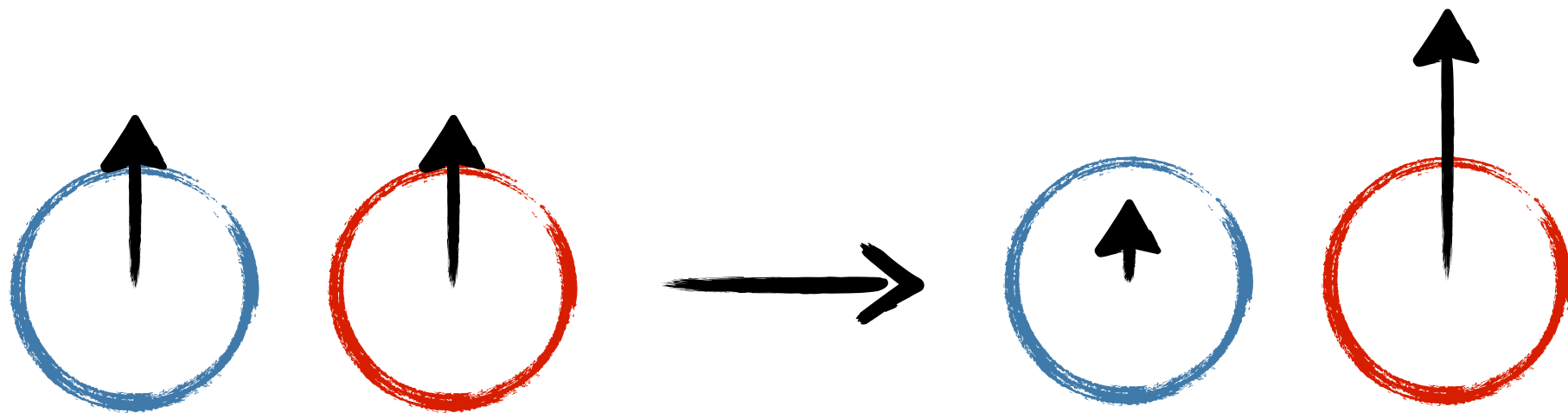


# THE TWIN HIGGS

NAIVE VACUUM:  $\langle H_A \rangle^2 = \langle H_B \rangle^2 = \frac{f^2}{2}$

$f$  IS NOT FAR FROM  $v$ , AND THE CUTOFF IS  $\sim \text{TeV}$ . NOT MUCH OF A PROTECTION, AND  $O(50\%)$  DEVIATIONS IN HIGGS COUPLINGS.

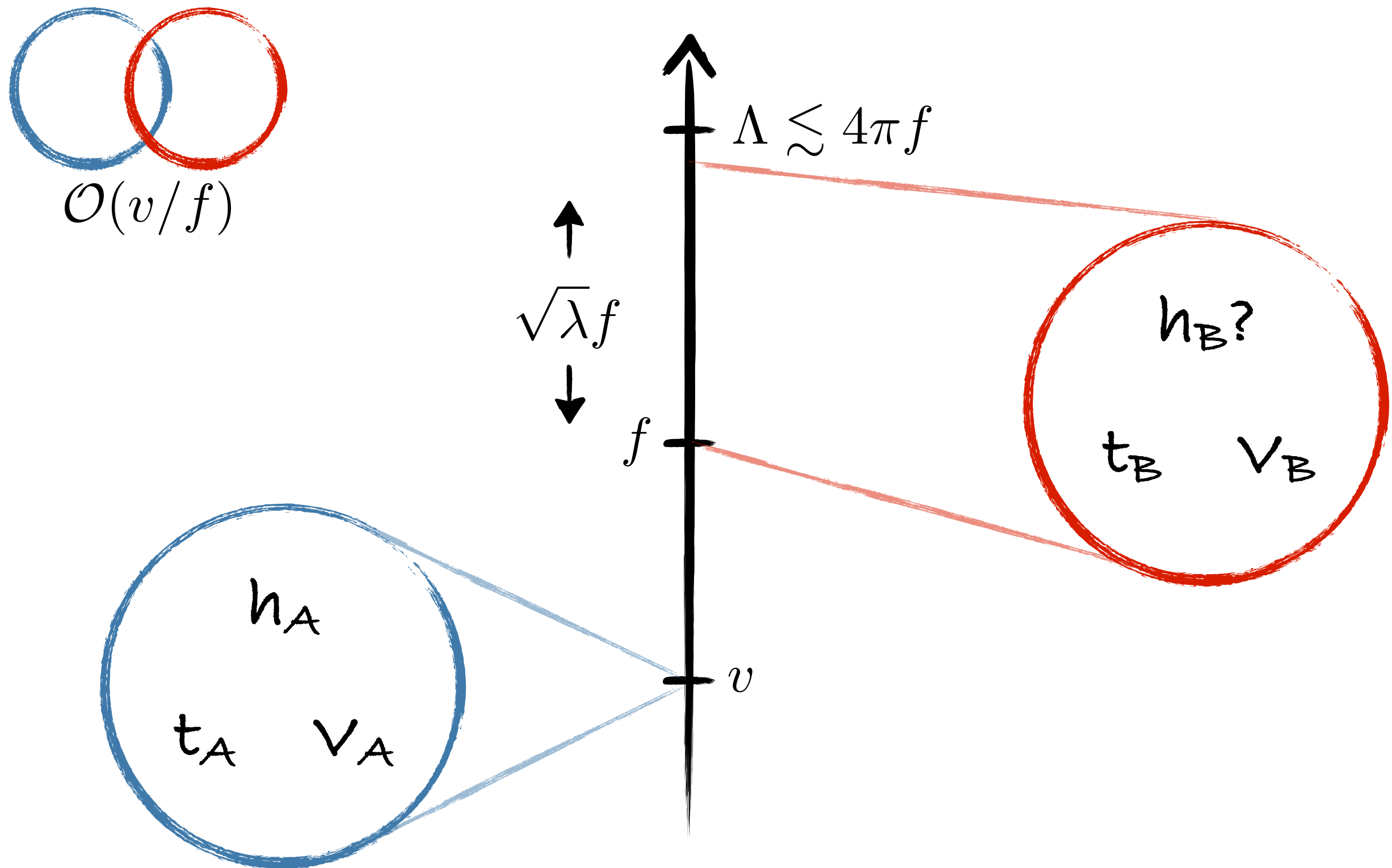
OPTION 1: SOFTLY BREAK  $Z_2$   $V_{soft}(H) = \delta m_H^2 |H_A|^2$   
 ALLOWS  $v \ll f$ , AT THE PRICE OF A TUNING  $\sim O(f^2/2v^2)$



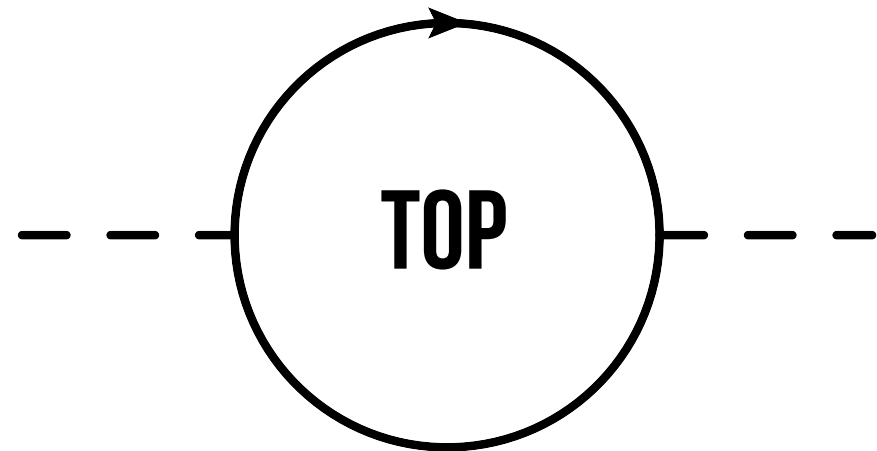
OPTION 2: HARD  
 BREAKING OF  $Z_2$

$$V_{hard}(H) = \delta_{A,B} |H_{A,B}|^4$$

# THE TWIN HIGGS



# THE TWIN TOP



THE TOP PARTNER ACTS AS EXPECTED FROM GLOBAL SYMMETRY PROTECTION, BUT NOT CHARGED UNDER QCD.

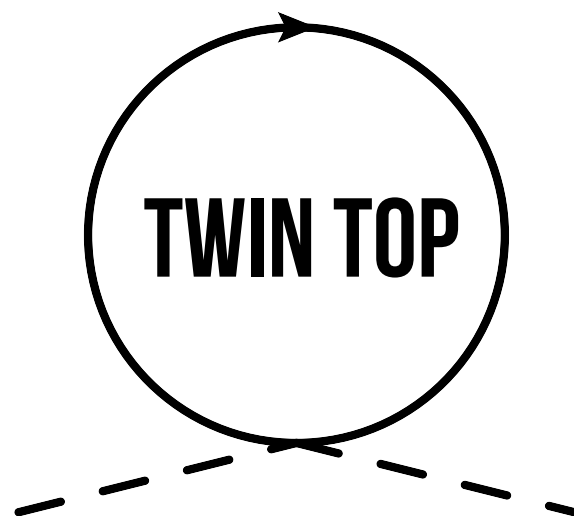
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$$\downarrow$$

$$h + \dots$$

$$\downarrow$$

$$f - \frac{h^2}{2f} + \dots$$



*NO DIRECT LIMIT ON TOP PARTNER.*

# WHERE ARE THE BODIES BURIED?

EVADES "TOP PARTNER THEOREM", BUT...

- DEMANDING EXACT  $Z_2$  MEANS **TWIN LIGHT GENERATIONS**; USELESS FOR NATURALNESS BUT TROUBLE FOR COSMOLOGY ( $N_{\text{EFF}}$ ).
- SYMMETRY STRUCTURE SLIGHTLY AWKWARD; REALLY ASKING FOR  $Z_2$  PLUS APPROXIMATE  $SU(4)$  OF HIGGS POTENTIAL.

*BIGGER QUESTION: JUST A PATHOLOGY, OR  
EXAMPLE OF DEEPER/GENERAL STRUCTURE?*

[KACHRU & SILVERSTEIN '98; BERSHADSKY & JOHANSEN '98, SCHMALTZ '99]

# ORBIFOLD FIELD THEORY

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- IF THE **PARENT** SYMMETRY PROTECTS THE HIGGS, OFTEN THE **DAUGHTER** DOES AS WELL, BUT WITHOUT THE FULL REPRESENTATIONS REQUIRED BY THE **PARENT**.

*SOUND FAMILIAR?*

# TWIN HIGGS IS AN ORBIFOLD

PARENT:  $SU(6) \times SU(4) / Z_2$

VARIOUS  $U(1)$  CHOICES:  $U(2)/Z_2$ ,  $U(1)^2/Z_2$ ,  $U(1)$ ; CANONICAL CHOICE  $U(1)^2/Z_2$

DAUGHTER:  $[SU(3) \times SU(2)]^2 \times S_2$

CANONICAL  $U(1)$  CHOICE:  $[SU(3) \times SU(2) \times U(1)]^2 \times S_2$

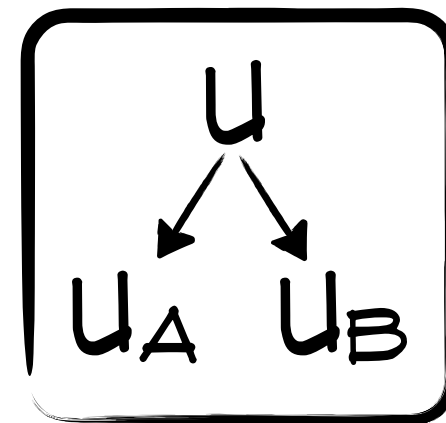
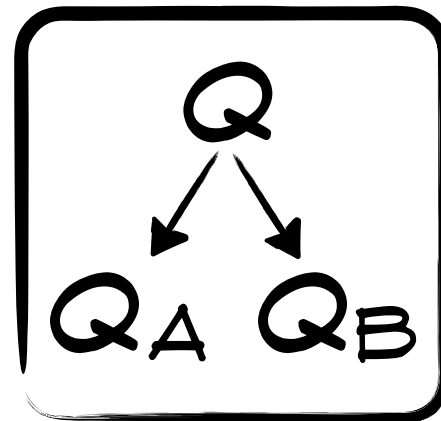
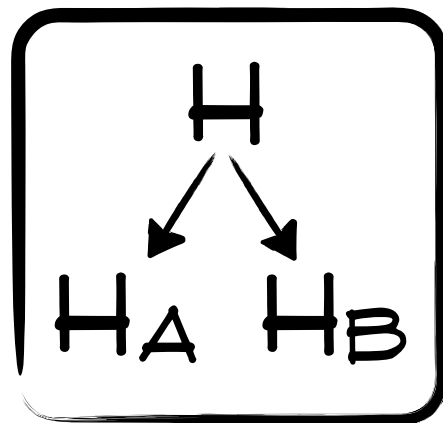
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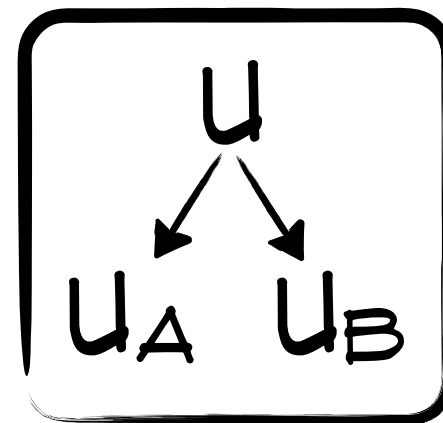
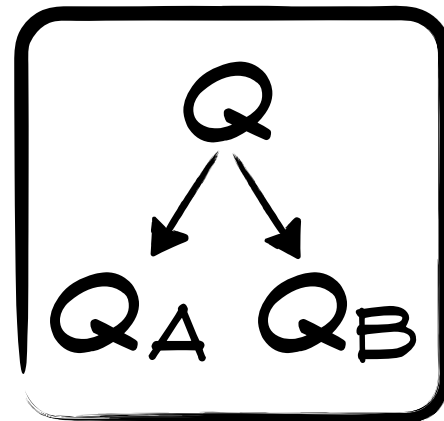
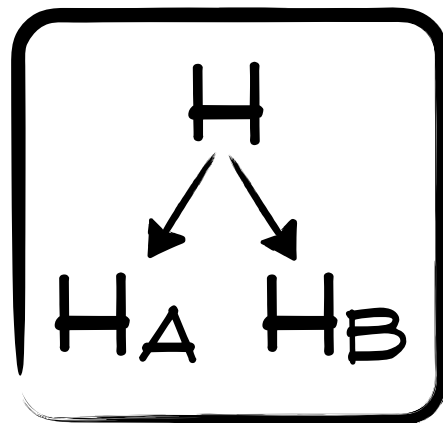
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$$HQU \begin{cases} \rightarrow H_A Q_A U_A \\ \rightarrow H_B Q_B U_B \end{cases}$$

$$|H|^4 \rightarrow (|H_A|^2 + |H_B|^2)^2$$

**GIVES YOU ALL THE COUPLINGS REQUIRED BY TWIN HIGGS.**

# UV COMPLETIONS

WE KNOW HOW TO THINK OF ORBIFOLDS  
GEOMETRICALLY...

$SU(6) \times SU(4)$

$[SU(3) \times SU(2)]^2$



$H, Q_3, U_3 (D_3?)$

$Q_{1,2}, U_{1,2}, D_{1,2} (D_3?)$

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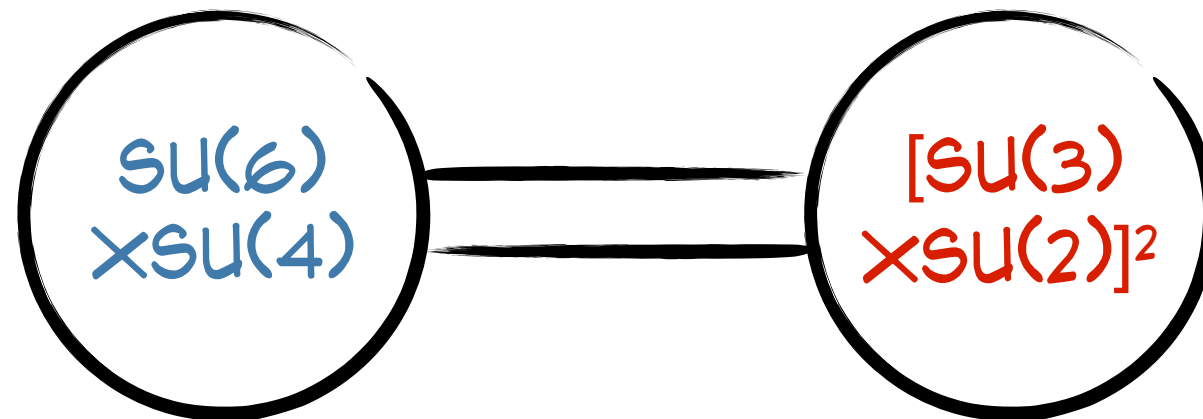
$$[SU(3) \times SU(2)]^2$$



$$H, Q_3, U_3 (D_3?)$$

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...OR BY DECONSTRUCTING THE GEOMETRY:



$$H, Q_3, U_3 (D_3?)$$

$$Q_{1,2}, U_{1,2}, D_{1,2} (D_3?)$$



# THE GENERALIZATION

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- THE OBVIOUS ABELIAN GENERALIZATION:  $\Gamma = Z_N$  INSTEAD OF  $Z_2$ . STRAIGHTFORWARD BUT BORING; N-HIGGS.
- SO WHAT ABOUT NON-ABELIAN DISCRETE SYMMETRIES? E.G.  $S_N, A_N$ , ETC. **EXPECT SOMETHING QUALITATIVELY NEW.**

# THE $S_3$ HIGGS

PARENT:  $SU(18) \times SU(12) / S_3$

DAUGHTER:  $[SU(3) \times SU(2)]^2 \times [SU(6) \times SU(4)]$

# THE $S_3$ HIGGS

PARENT:  $SU(18) \times SU(12) / S_3$

DAUGHTER:  $[SU(3) \times SU(2)]^2 \times [SU(6) \times SU(4)]$

$L = HQU$

	SU(2)	SU(2)	SU(4)
$H_A$	$\square$		
$H_B$		$\square$	
$H_C$			$\square$
$H_D$			$\square$

	SU(3)	SU(3)	SU(6)
$u_A$	$\bar{\square}$		
$u_B$		$\bar{\square}$	
$u_C$			$\bar{\square}$
$u_D$			$\bar{\square}$

	3x2	3x2	6x4
$Q_A$	$\square \bar{\square}$		
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$Q_C$			$\square \bar{\square}$

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$$L = HQU$$

	SU(2)	SU(2)	SU(4)
$H_A$	$\square$		
$H_B$		$\square$	
$H_C$			$\square$
$H_D$			$\square$

	SU(3)	SU(3)	SU(6)
$u_A$	$\bar{\square}$		
$u_B$		$\bar{\square}$	
$u_C$			$\bar{\square}$
$u_D$			$\bar{\square}$

	3x2	3x2	6x4
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$Q_C$			$\square \bar{\square}$

"HIGGS IS PSEUDO-GOLDSTONE OF THE ORBIFOLDED  
SU(12) SYMMETRY"

# HOW TO NORMALIZE YOUR ORBIFOLD HIGGS

NOT AT ALL OBVIOUS THAT RADIATIVE  
CORRECTIONS PRESERVE THE  $SU(12)$ ! BUT  
ORBIFOLD CORRESPONDENCE DEMANDS IT...



# HOW TO NORMALIZE YOUR ORBIFOLD HIGGS

NOT AT ALL OBVIOUS THAT RADIATIVE  
CORRECTIONS PRESERVE THE  $SU(12)$ ! BUT  
ORBIFOLD CORRESPONDENCE DEMANDS IT...

GIVEN PARENT COUPLINGS  $g, Y, \lambda$ ,

FIELD THEORY ORBIFOLD + CANONICAL  
NORMALIZATION OF DAUGHTER STATES  $\rightarrow$   
 $d_\alpha$  DAUGHTER SECTOR INHERITS COUPLINGS

$$g \rightarrow \frac{g}{\sqrt{d_\alpha}}$$

$$Y \rightarrow \frac{Y}{\sqrt{d_\alpha}}$$

$$\lambda \rightarrow \lambda$$

# QUADRATIC SENSITIVITY

CW POTENTIAL FOR SCALAR TRANSFORMING AS A  
FUNDAMENTAL UNDER  $SU(2_{d_\alpha})$  WITH APPROPRIATE YUKAWA:

$$\delta m_{H_\alpha}^2 = \frac{\Lambda^2}{16\pi^2} \left[ -6d_\alpha y_\alpha^2 + 3 \left( d_\alpha - \frac{1}{4d_\alpha} \right) g_\alpha^2 + \dots \right]$$

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TOTAL ONE-LOOP CW POTENTIAL FOR  $S_3$  HIGGS SCALARS:

$$\propto \frac{\Lambda^2}{16\pi^2} \left[ -6Y^2 + 3g^2 + \dots \right] (|H_A|^2 + |H_B|^2 + |H_C|^2 + |H_D|^2)$$

SU(12) INVARIANT ↗

~1/N ORBIFOLD CORRECTIONS →  $-\frac{3\Lambda^2}{256\pi^2} g^2 (|H_C|^2 + |H_D|^2)$

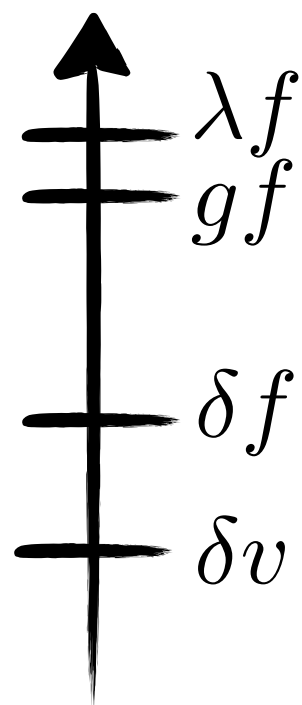
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3+3+15=21 EATEN, 2 PSEUDOS REMAIN

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IN TYPICAL VACUUM  $v \sim f$  & PSEUDOS ONLY PARTIALLY  
ALIGNED W/SM VEV. AS IN TWIN HIGGS, NEED TO TILT  
POTENTIAL TO GET  $v \ll f$  & ONE SM-LIKE PSEUDO.



RADIAL MODE,  $M \sim \lambda f$

MOST HIGGSSES EATEN,  $M \sim g f$

ONE GENERIC PSEUDO,  $M \sim \delta f$

ONE SM-LIKE PSEUDO,  $M \sim \delta v$

# THE $A_4$ HIGGS

PARENT:  $SU(36) \times SU(24) / A_4$

DAUGHTER:  $[SU(3) \times SU(2)]^3 \times [SU(9) \times SU(6)]$

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$3 \times$

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$H \quad Q \quad U$

+

$SU(9) \times SU(6)$

$H_1 \ H_2 \quad U_1$   
 $H_3 \quad U_2 \ U_3 \quad Q$



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$SU(24) \rightarrow SU(23)$ : 41 (PSEUDO)GOLDSTONES.  
 $3+3+3+35=44$  EATEN, 3 PSEUDOS REMAIN

"HIGGS IS PSEUDO-GOLDSTONE OF THE ORBIFOLDED  
 $SU(24)$  SYMMETRY"

# REALISTIC MODELS

I'VE JUST SKETCHED TOY MODELS FOCUSING ON THE HIGGS POTENTIAL; FOR REALISTIC MODELS (E.G. HIGHER-DIM THEORIES), WE...

- NEED TO MAKE CHOICES FOR  $B_R$ ; EITHER PART OF PARENT SYMMETRY (NEED 2HDM) OR NOT (LIVES AT DEFECT).
- NEED TO MAKE CHOICES FOR FIRST/SECOND GENERATIONS; SIMPLEST CHOICE IS TO LIVE AT DEFECT.
- NEED TO DEAL WITH ANOMALIES OF PARENT AND DAUGHTER SYMMETRIES.

*NONE OF THESE ARE DEAL-BREAKERS, BUT IT HELPS TO DRESS THE FIELD THEORY ORBIFOLD.*

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- PHENOMENOLOGY OF GEOMETRIC TWIN HIGGS CAN CHANGE RADICALLY!
- THERE ARE ***MANY MORE THEORIES OF THIS TYPE***, WITH HIDDEN SECTORS NOT SIMPLY RELATED TO THE STANDARD MODEL!



# THE BIG PICTURE

- INTENSE DEBATE ABOUT NATURALNESS POST-HIGGS, MANY CONCLUSIONS BEING DRAWN.
- BUT WE'RE FAR FROM WRITING DOWN ALL NATURAL THEORIES USING SYMMETRIES. MAJOR LOOPHOLES IN "TOP PARTNER THEOREM."
- WE SHOULD TRY REDUCTIONS OF ALL SYMMETRY SOLUTIONS TO THE HIERARCHY PROBLEM. ORBIFOLDS OF GLOBAL SYMMETRY ONLY ONE AVENUE -- ORBIFOLDS ALSO OF R-SYMMETRY? ORIENTIFOLDS? OTHER STRINGY SINGULARITIES?

*LOTS TO EXPLORE BEFORE WE PASS  
JUDGMENT ON NATURALNESS!*